

## Exercise 1

**Assignment 1. (4/5)** Radial distribution function (RDF) is a statistical measure of microsolvation structure. Among other definitions, it is defined as an ensemble average

$$g_{ab}(r) = \frac{V}{N^2} \left\langle \sum_i \sum_{j \neq i} \delta(\mathbf{r} - \mathbf{r}_{ij}) \right\rangle.$$

A numerical recipe for calculation of  $g_{ab}(r)$  includes steps

- Choose  $r_{min}$ ,  $r_{max}$  and  $\Delta r$ , and generate grid points  $\{r_i\}$ ,  $i = 1, \dots, N_{grid}$ .
- Generate a histogram  $h_{ab}^{(c)}(i)$ ,  $i = 1, \dots, N_{grid}$ ,  $c = 1, \dots, N_{conf}$ , counting the number of times the two atoms of type  $a$  and  $b$  lies between  $r_i$  and  $r_{i+1}$ . Use all atoms of proper type in the snapshot, one histogram for each snapshot (total  $N_{conf}$ ) to obtain best possible statistics. As we are dealing with bulk, one has to include pbc and minimum image convention.
- Once the histograms  $h_{ab}^{(c)}$  have been generated, normalize them point-by-point (for each  $r_i$ ,  $i = 1, \dots, N_{grid}$ )

$$g_{ab}^{(c)}(r_i) = \frac{h_{ab}^{(c)}(i)}{4\pi\rho_b r_i^2 \Delta r N_a},$$

where  $\rho_b$  is the number density ( $N_b/V$ ) of atoms of type  $b$ , and  $N_a$  is the number of atoms of type  $a$ , you used in generating histogram  $h_{ab}^{(c)}(i)$ .

- To account for a varying box size, calculate  $g_{ab}(r)$  as the average over  $g_{ab}^{(c)}(r)$  of snapshots  $c = 1, \dots, N_{conf}$ .

Prepare a code that reads in *mystery.xyz* of the previous exercise and calculates  $g_{OO}(r)$  from it using periodic boundary conditions in all three dimensions. Play a bit with the bin size  $\Delta r$  and select a reasonable one. Include the source code as a separate file, and attach a plot of your result in the report. **Note you can use any programming language you know. With MATLAB this code took approximately 80 lines.**

**Turn the page! →**

**Assignment 2. (1/5)** Please answer.

- By definition, all RDFs should  $g(r) \rightarrow 1$ , when  $r \rightarrow \infty$ . Give this an verbal (written) interpretation based on the RDF you just calculated. How far ( $r$ -wise) is it reasonable to calculate the RDF in the given case?
- Based on the RDF you just calculated, what would be your first guess for the distance of the minimum in the potential energy curve for O-O? Neglect dependence on molecular orientations here, but in future remember that they naturally play a role.
- In this exercise we studied a system in a cubic unit cell. How should the minimum image vector be calculated in a case of orthorhombic (rectangular) box of side lengths  $L_x$ ,  $L_y$  and  $L_z$ ?

Return your solutions to Ville *moleculardynamicssimulations@gmail.com*, **latest Wed 18.9.2013 10:15**. To maintain good relations with the assistant, you might want to consider sending a single PDF with all your solutions and then your code as a separate file.